

5. RADIOACTIVITY - DECAYS

Natural radioactivity was accidentally discovered by Becquerel in 1896, who found a photographic plate blackened by the proximity of a uranium compound. Radioactivity was investigated by Rutherford. He found the radiation consisted of two kinds namely the α -ray and the β -ray. Villard later discovered a third ray which he called the Gamma radiation.

A small amount of radioactive salt is placed at the bottom of a narrow hole drilled in a lead block. The rays escape from the lead block in a narrow pencil. The whole arrangement is enclosed in a box which can be evacuated. A magnetic field is applied at right angles to the beam of rays. The α -rays and β -rays are deflected, but the gamma rays are not deflected.

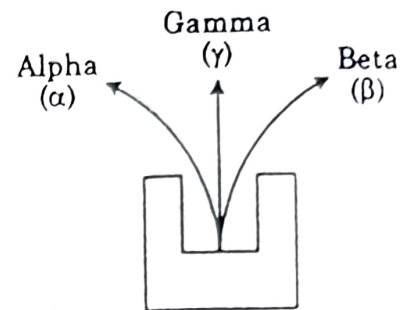


Fig. 15

The $\left[\frac{e}{m} \right]$ of the Beta rays was measured by Becquerel in 1900. The following year Kaufmann carried out a more precise measurement. These experiments showed that Beta rays were streams of electrons. Later Bucherer proved that the mass of the electron varied according to the formula $m = \frac{m_0}{\left[1 - \frac{v^2}{c^2} \right]^{1/2}}$

Rutherford and Robinson measured the $\frac{e}{m}$ for α -rays by deflections in electric and magnetic fields. The charge on the alpha particle was measured by Rutherford and Geiger as well as by Regener. The α -particle was found to have a mass four times the mass of the hydrogen atom and a positive charge equal to twice the charge on the electron.

This was confirmed by Rutherford and Royds.

Effect of Radioactive Decay

If an atom of charge Z and mass A emits an alpha particle, the following change occurs:

$$Z \longrightarrow Z - 2$$

$$A \longrightarrow A - 4$$

The emission of a beta particle from the nucleus raises the positive nuclear charge by unity while the mass remains unchanged.

$$Z \longrightarrow Z + 1$$

The unstable nucleus undergoes a spontaneous change in its charge, by the transformation of a neutron into a proton with the emission of an electron.

Decay Laws

The number of unstable nuclei remaining undecayed in a given sample decreases exponentially with time.

$$N = N_0 e^{-\lambda t}$$

where N_0 is the number of unstable nuclei present at an arbitrary instant of time $t = 0$. λ is called the decay constant which depends on the nuclide.

The activity of a sample is the number of decays per unit time.

$$R = -\frac{dN}{dt} = \lambda N_0 e^{-\lambda t} \\ = \lambda N(t)$$

λdt represents the probability that a given nucleus will decay in time dt .

The decay of a nucleus is a random process, impossible to predict on the basis of the history of the nucleus. However a mean lifetime τ can be defined. If $v(t) dt$ is the number disintegrating in the time interval between t and $t + dt$,

$$N_0 \tau = \int_0^{\infty} t v(t) dt$$

$$v(t) dt = \lambda N(t) dt \text{ from (14)} \\ = \lambda N_0 e^{-\lambda t} dt$$

$$\therefore \tau = \frac{1}{\lambda}$$

Thus meanlife is the reciprocal of the decay constant.

If a certain unstable nucleus is present at a given instant, then the mean life time signifies how much longer we can statistically expect the nucleus to survive.

Half-life is the time that must elapse for the activity to fall to one-half of its present value.

$$t_{1/2} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda} = 0.693 \tau$$

Branched decays

More than one decay process is possible for a given unstable nucleus in a given state. For each process, we may define a partial decay constant $\lambda_1, \lambda_2, \dots$. The total probability of decay per unit time is

$$\lambda = \lambda_1 + \lambda_2 + \dots$$

Similarly,

$$\tau = \frac{1}{\lambda_1 + \lambda_2 + \dots}$$

Unit of Activity $\left(R = -\frac{dN}{dt} \right)$ is 1 becquerel = 1 Bq. 1 Bq = 1 event/s. The activities in practice are so high that larger units are required.

$$1 \text{ MBq} = 10^6 \text{ Bq}$$

$$1 \text{ GBq} = 10^9 \text{ Bq}$$

$$1 \text{ curie} = 1 \text{ Ci} = 3.70 \times 10^{10} \text{ event/s} = 37 \text{ GBq}$$